

# Method for a Comprehensive Analytical Study of Contact Pressures, Wear, and Durability of Metal-Polymer Helical and Spur Gears with Steel Pinion and Polyamide Gear

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## ABSTRACT

An analytical complex study of metal-polymer (MP) helical and spur gears by a new author's analytical method was carried out. The influence of the helix angle on the contact pressures in the engagement, the teeth wear, and the durability of the MP gears of different polymers has been established. MP gears with a pinion made of carbon steel (0.45% C) and gear made of basic polyamides PA6, PA66, and their composites with the following fillers: fiberglass (PA6+30GF), carbon fiber (PA6+30CF), molybdenum disulfide (PA6+MoS<sub>2</sub>), and oil filled cast polyamide (PA6+Oil) are studied. According to the developed procedure for determination of the angles of engagement parity change, it is shown that there is two-one-two-pair or three-two-three-pair engagement depending on the helix angle. Quantitative and qualitative regularities of changes in the initial maximum contact pressures and their reduction due to tooth wear over the time from the moment of the entrance of teeth to engagement up to their exit from it are established. In particular, at a helix angle of  $\beta = 10^\circ$ , the contact pressures reduce to 33% compared to spur gears. The linear wear of the gear polymer tooth profile  $h_{2j}$  at selected points of engagement and different helix angles has been investigated, and the influence of the pressure angle on it is shown. It is established that its regularities of change during the engagement phase are the same for all polymeric materials studied. The durability of transmissions is calculated, and its comparative evaluation is given. At the helix angle  $\beta = 5^\circ$ , a slight increase in durability is achieved compared to spur gears, and at  $\beta = 10^\circ$  the durability of MP gears increases by about 1.5 times for all polymeric materials studied.

## 1. INTRODUCTION

The use of polymeric materials in metal-polymer (MP) gears operating in friction conditions without lubrication is quite common, in particular polyamides both unreinforced (PA6, PA66) and composites with different fillers (glass and carbon fiber, molybdenum disulfide, graphite, carbonite, bronze powder, polyethylene, PTFE, oil, etc.) and different volume content. It is known that in such a way it is possible to improve their mechanical properties, especially wear resistance. Accordingly, the durability of MP gears will also increase. Common polymeric materials for MP gears are polyamide PA6 and its composites PA6+30GF, PA6+30CF, PA6+MoS<sub>2</sub>, and PA6+Oil, thanks to their good mechanical, technological, operational, and tribological properties.

An urgent task of triboengineering is to meet the challenges of engineering practice with the development of computational and numerical methods for research of MP and polymer gears for their contact strength, wear resistance, and durability. However, despite the urgency of solving this important for science and engineering problem in connection with the growing use of these types of polymer gears, effective calculation methods for assessing their performance have not yet been developed. Previously, in using a simplified calculation method [2] based on Archard's law of abrasive wear, a partial study of MP spur gears with a gear made of PA6+30GF, PA6+30CF with dispersed fibers has been conducted [1]. As for studies of MP gears by different numerical methods for their wear resistance and durability, they have not yet been carried out.

In [3], the behavior of a number of polymers and polymer composites was studied. Acetal PA6 was the best of the unreinforced polymers. The wear of the studied materials was significantly differentiated. In some works [4,5], there are results of calculation of contact and bending tooth strength of MP spur gears. The influence of the load distribution among the gears on the specified stresses in the MP gears with a PA66 polyamide gear paired with a steel pinion has been established in [4]. And in [5], the maximum contact pressures of the same gears have been estimated.

The previous tribological studies of polymeric materials for gears have yielded different results. In particular, experimental studies of the volumetric tooth wear of model MP gears were conducted in [6-8]. Gears made of PA6-Mg, PA6-Na, PA66+30GF paired with S355 steel in the presence of abrasive and without it were studied in [6,7]. The wear of gears made of PA6 was studied in [8] for various types of MP gears (spur, bevel, and worm).

The tribological behavior of different types of polyamides for MP gears paired with steel has been studied on a pin-on-disk testing machine. In particular, work [9] is devoted to the wear resistance of the tribocouple PA66 - steel SAE 1045, used in clutch discs. Also, in [10-12] the tribological behavior of PA6 polyamide during dry friction was studied under different operation conditions.

A number of works are devoted to the experimental study of polymer gear wear, in particular, gears made of polyamides and their composites [13-19]. In [13], the tribological behavior of wheels made of PA6, PA66, PA46, and PA12, reinforced with carbon fiber was studied. Accelerated tests of polymer gears [14] were performed on 15 different compositions filled with glass or carbon fiber and unfilled PA6, PA66, and POM. A detailed study on the friction and wear of gears made of acetal POM and PA6 in the same type and mixed pairs was described in [15]. PA6 filled with fiberglass and Teflon was studied in [16]. The work [17] is devoted to the wear of 27 pairs of gears made of PA66, PA66+15GF, and PA66+30GF. In [18], the wear resistance of polymer gears made of PA66, polyester PEEK, and POM at different loads and speeds has been investigated. The work [19] contains the results of testing the wear of gears made of PA filled with 30% glass or 25% SiC, PA6 with 25% SiC, and PA66 with 25% SiC.

However, the results of the wear resistance studies of polymeric materials on tribo-testers according to the pin-on-disk scheme or other standardized schemes of sliding friction, as well as on model gears are difficult to use when calculating gears for durability. The main reason for such difficulty is conducting research at one value of load (tribotesting machine) or one torque (model gears), and thus the obtained Archard's coefficient of abrasion cannot be used at other loads.

Therefore, an urgent scientific and engineering problem is the development of effective methods for estimating the wear and service life of gears made of polymer composite materials, which take into account the results of representative model tribo-experimental studies in modeling the kinetics of wear. Accordingly, in [20-24] the author's method of MP gears calculation based on the phenomenological methodology of wear resistance research of materials at sliding friction [20,25-28] by frictional-fatigue wear mechanism is given. This approach is fundamentally different from the current approach to the mechanism of wear of metal-polymer and polymer tribocouples, which adopts Archard's law for adhesive-abrasive wear.

It should be noted that statistical data on the causes of the functional capacity loss of various tribomechanical systems indicate that the main reason in 85 - 95% of cases is the wear of their elements, which is generally known. The teeth failures of MP gears operating under dry friction conditions, such as breakage near the root, chipping at the edge, increased plastic deformation or local fatigue failure (pitting) occur much less often and are usually caused by non-compliance with the loading or temperature regime of operation.

The aim of this work is to mathematically model the contact and tribocontact interaction in the meshing of a metal-polymer spur gear. According to the developed new generalized author's method, the article studies the contact strength (load carrying capacity), wear, and service life of helical and spur gears with a gear made of polyamides PA6, PA66, and composites PA6+30GF, PA6+30CF, PA6+MoS<sub>2</sub>, and PA6+Oil. Changes in contact parameters due to tooth wear and changes in their parity of engagement. There have been described no methods in the literature to solve the problem of studying MP gears in such a statement.

## 2. METHOD FOR STUDY OF WEAR AND DURABILITY OF HELICAL AND SPUR GEARS

The general view of MP gears is given in Fig. 1.

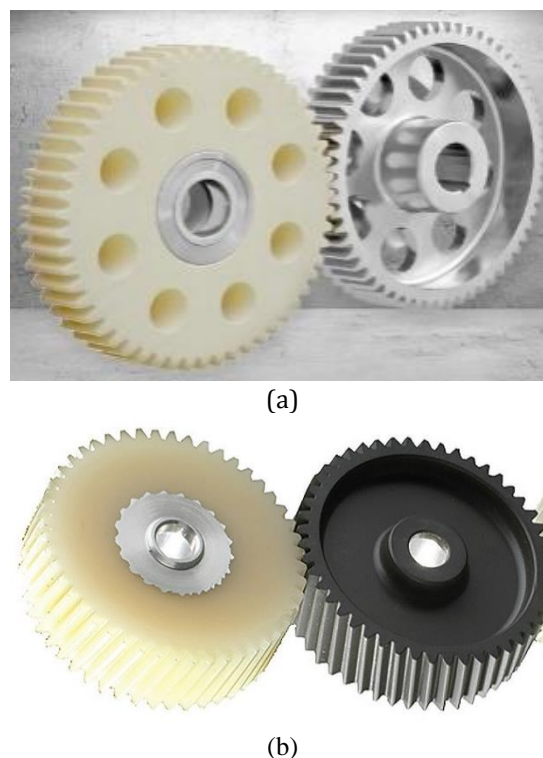


Fig. 1. Metal-polymer gears: (a) helical, (b) spur.

When calculating helical gears, the following characteristics should be determined:

- initial maximum contact pressures  $p_{j\max}$  at any  $j$ -th point of the tooth profile;
- maximum contact pressure  $p_{jh\max}$  due to tooth wear;
- gear polymer tooth linear wear  $h_{2j}$  at any  $j$ -th point of the profile;
- minimum gears durability  $t_{min}$ .

### 2.1. Function of linear wear of teeth

With taking into account the peculiarities of teeth' contact during their interaction, the function of their linear wear  $h'_{kj}$  can be expressed by the formula (1). This formula is used for calculation of helical gears at any  $j$ -th point of tooth profile over a single time  $t'_j$  of tribocontact in a one-pair engagement [23-26,28]:

$$h'_{kj} = \frac{v_j t'_j (\hat{f} p_{j\max})^{m_k}}{C_k (0.5R_m)^{m_k}} = \frac{v_j t'_j (\tau_{j\max})^{m_k}}{C_k (\tau_S)^{m_k}}, \quad (1)$$

where  $t'_j = 2b_j / v_0 = \text{var}$ ;  $v_0 = \omega_1 r_1 \sin \alpha_t$ ;  $\tau_{j\max} = \hat{f} p_{j\max}$ .

## 2.2. Contact parameters

The initial maximum contact pressures  $p_{j\max}$  and the contact area width  $2b_j$  at the  $j$ -th point of the profile are calculated by Hertz's formulas

$$\begin{aligned} p_{j\max} &= 0,564\sqrt{N'/\theta\rho_j}, \\ 2b_j &= 2,256\sqrt{\theta N'\rho_j}, \end{aligned} \quad (2)$$

where  $N' = N / l_{\min} w$ ;  $N = T_{nom} K_g / r_1 \cos \alpha_t$ ;  $T_{nom} = 9550P / n_1$ ;  $\theta = (1 - \mu_1^2) / E_1 + (1 - \mu_2^2) / E_2$ .

The initial radii of curvature of tooth profiles at the  $j$ -th point of helical gear (reduced radius  $\rho_j$ , for a pinion  $\rho_{1j}$ , for a gear  $\rho_{2j}$ )

$$\rho_j = \frac{\rho_{1j}\rho_{2j}}{\rho_{1j} + \rho_{2j}}, \rho_{1j} = \frac{\rho_{t1j}}{\cos \beta_b}, \rho_{2j} = \frac{\rho_{t2j}}{\cos \beta_b}, \quad (3)$$

where

$$\begin{aligned} \beta_b &= \arctan(\tan \beta \cos \alpha_t), \alpha_t = \arctan\left(\frac{\tan \alpha}{\cos \beta}\right), \\ \rho_{t1j} &= r_{b1} \tan \alpha_{t1j}, \rho_{t2j} = r_2 \sqrt{(r_{2j} / r_2)^2 - \cos^2 \alpha_t}, \\ \alpha_{t1j} &= \arctan(\tan \alpha_{t10} + j \Delta \varphi), \\ \alpha_{t2j} &= \arccos\left[\left(r_2 / r_{2j}\right) \cos \alpha\right], r_{b1} = r_1 \cos \alpha_t, \\ r_{b2} &= r_2 \cos \alpha_t, r_1 = m z_1 / 2 \cos \beta, \\ \tan \alpha_{t10} &= (1 + u) \tan \alpha_t - \frac{u}{\cos \alpha_t} \sqrt{(r_{20} / r_2)^2 - \cos^2 \alpha_t}, \\ r_{20} &= r_{a2} - r, r_{a2} = r_2 + m, \\ r_{2j} &= \sqrt{a^2 + r_1^2 - 2 a r_{1j} \cos(\alpha_t - \alpha_{t1j})}, \\ r_{1j} &= r_1 \cos \alpha_t / \cos \alpha_{t1j}, a = (z_1 + z_2) m / 2 \cos \beta, \\ \tan \alpha_{t1s} &= \arctan \sqrt{(r_{1s} / r_1)^2 - \cos^2 \alpha_t}, r_{1s} = r_{a1} - r, \\ r_{a1} &= r_1 + m, \\ \tan \alpha_{t2s} &= (1 + u^{-1}) \tan \alpha_t - \\ & - \frac{1}{u \cos \alpha_t} \sqrt{(r_{1s} / r_1)^2 - \cos^2 \alpha_t}. \end{aligned}$$

The minimum length of the contact line

$$l_{\min} = \frac{b \varepsilon_\alpha}{\cos \beta_b} \left[ 1 - \frac{(1 - n_\alpha)(1 - n_\beta)}{\varepsilon_\alpha \varepsilon_\beta} \right] \text{ at } n_\alpha + n_\beta > 1,$$

$$l_{\min} = \frac{b \varepsilon_\alpha}{\cos \beta_b} \left[ 1 - \frac{n_\alpha n_\beta}{\varepsilon_\alpha \varepsilon_\beta} \right] \text{ at } n_\alpha + n_\beta \leq 1, \quad (4)$$

$$\begin{aligned} \text{where } \varepsilon_\alpha &= \frac{z_1(e_1 + e_2)}{2\pi r_{b1}}, \varepsilon_\beta = \frac{b \sin \beta}{\pi m}, \\ e_1 &= \sqrt{r_{1s}^2 - r_{b1}^2} - r_1 \sin \alpha_t, e_2 = \sqrt{r_{20}^2 - r_{b2}^2} - r_2 \sin \alpha_t. \end{aligned}$$

Contact parameters such as the contact wear pressures  $p_{jh\max}$  and the tribocontact width  $2b_{jh}$  are calculated considering the tooth wear according to the modified Hertz formulas

$$\begin{aligned} p_{jh\max} &= 0,564\sqrt{N'/\theta\rho_{jh}}, \\ 2b_{jh} &= 2,256\sqrt{\theta N'\rho_{jh}}, \end{aligned} \quad (5)$$

$$\text{where } \rho_{jh} = \frac{\rho_{1jh}\rho_{2jh}}{\rho_{1jh} + \rho_{2jh}}.$$

The variable radii of curvature  $\rho_{kjh}$  are calculated by our method described in [22,26-28].

## 2.3. Sliding speed in engagement

The sliding speed is calculated as follows

$$v_j = \omega_1 r_{b1} (tg \alpha_{t1j} - tg \alpha_{t2j}). \quad (6)$$

## 2.4. Changing the parity of teeth

The angle  $\Delta\varphi_{1F_2}$  of the tooth entrance to the one-pair engagement and the angle  $\Delta\varphi_{1F_1}$  of the exit from it are determined by the relations:

$$\Delta\varphi_{1F_2} = \varphi_{10} - \varphi_{1F_2}, \Delta\varphi_{1F_1} = \varphi_{10} + \varphi_{1F_1}, \quad (7)$$

where

$$\begin{aligned} \varphi_{1F_2} &= \tan \alpha_{F_2} - \tan \alpha_t, \varphi_{1F_1} = \tan \alpha_{F_1} - \tan \alpha_t, \\ \varphi_{10} &= \tan \alpha_{t10} - \tan \alpha_t, p_b = \pi m \cos \alpha_t / \cos \beta; \\ \tan \alpha_{F_2} &= \frac{r_1 \sin \alpha_t - (p_b - e_1) + 0.5 p_b n_\beta}{r_1 \cos \alpha}, \\ \tan \alpha_{F_1} &= \frac{r_1 \sin \alpha_t - (p_b - e_2) - 0.5 p_b n_\beta}{r_1 \cos \alpha}. \end{aligned} \quad (8)$$

The angle  $\Delta\varphi_{1E}$  of the tooth exit from the engagement

$$\Delta\varphi_{1E} = \varphi_{10} + \varphi_{1E}, \quad (9)$$

where  $\varphi_{1E} = \tan \alpha_E - \tan \alpha_t$ ,  $\alpha_E = \arccos(r_{b1} / r_{1s})$ .

In the case of three-two-three-pair tooth engagement, when  $2 \leq \varepsilon_\gamma = \varepsilon_\alpha + \varepsilon_\beta < 3$ , relations (8) can be used only if the fractional parts  $n_\alpha, n_\beta$  of the coefficients  $\varepsilon_\alpha, \varepsilon_\beta$  of the end and pitch overlap correspond to the relation  $n_\alpha + n_\beta < 1$ . If  $n_\alpha + n_\beta \geq 1$ , they do not yield the correct values of angles  $\Delta\varphi_{1F2}$  and  $\Delta\varphi_{1F1}$ . Then the following expressions to determine  $\tan \alpha_{F2}$  and  $\tan \alpha_{F1}$  should be used:

$$\begin{aligned} \tan \alpha_{F2} &= \frac{r_1 \sin \alpha_t - (p_b - e_1) + 0.5 p_b (1 - \varepsilon_\beta)}{r_1 \cos \alpha} \\ \tan \alpha_{F1} &= \frac{r_1 \sin \alpha_t - (p_b - e_2) - 0.5 p_b (1 - \varepsilon_\beta)}{r_1 \cos \alpha} \end{aligned} \quad (10)$$

### 2.5. Durability of gears

To solve the problem of durability of gears, our before-developed block scheme of calculation [22-26,28] was used. For the number of revolutions of the pinion  $n_{1s}$  and the gear  $n_{2s}$ , which corresponds to the number of interaction blocks  $B$  of the accepted size under constant contact conditions, the total tooth wears  $h_{1jn}$  and  $h_{2jn}$  at the  $j$ -th points of contact are determined as follows:

$$h_{1jn} = \sum_1^{n_{1s}} h_{1jB}, \quad h_{2jn} = \sum_1^{n_{2s}} h_{2jB} \quad (11)$$

where  $n_{2s} = n_{1s} / u$ ;  $h_{kjB} = \sum h'_{kj}$  is the tooth wear in each block of interaction.

When the initial contact pressures  $p_{j\max}$  change because of tooth wear, the duration of the gear operation  $t_B$  at the number of revolutions  $n_{1s}$  or  $n_{2s}$  of toothed wheels is calculated as follows:

$$t_B = n_{1s} / 60n_1 = n_{2s} / 60n_2. \quad (12)$$

### 3. NUMERICAL SOLUTION AND DISCUSSION

Involute helical and spur MP gears with steel pinions and polymer gears were studied.

#### Initial data

$T_{nom} = 4000$  Nmm,  $n_1 = 700$  rpm;  $B = 420,000$  rev (10 hours of operation);  $K_g = 1.2$ ;  $m = 4$  mm,  $u = 3$ ,  $z_1 = 20$ ,  $z_2 = 60$ ,  $b = 50$  mm,  $\beta = 0^\circ, 5^\circ, 10^\circ$ ,  $h_{2*} = 0.5$  mm.

#### Materials

Pinion: carbon steel 0.45% C, normalization, grinding,  $E_1 = 2.1 \cdot 10^5$  MPa,  $\mu_1 = 0.3$ ;  $C_1 = 10^9$ ,  $m_1 = 2$ ;  $\tau_{S1} = 345$  MPa.

Gear: polyamides (PA) and composites based on them (Table 1).

**Table 1.** Characteristics of polyamides and composites used.

Characteristics	Thermoplastic polymeric materials					
	PA6 (Sustamid 6 Rochling)	PA66 (Sustamid 66 Rochling)	PA6+ 30GF (Sustamid 6 GF30 Rochling)	PA6+ MoS <sub>2</sub> (Sustamid 6 MO Rochling)	PA6+30CF (Sustamid 6 ESD 60 Rochling)	PA6+ Oil (Sustamid 6 OL Rochling)
Young's modulus $E_2$ , MPa	2000	2300	2700	1660	3300	1960
Poisson's ratio $\mu_2$	0.4	0.4	0.41	0.4	0.41	0.4
Friction coefficient $f$	0.23	0.23	0.31	0.23	0.25	0.25

Note: PA6+30GF – fiberglass filler (30 vol% of fine fibers), PA6+30CF – carbon fiber (30 vol% of fine fibers), PA6+MoS<sub>2</sub> – molybdenum disulfide, PA6+Oil – oil-filled cast polyamide.

The coefficient of friction was determined by experimental studies of the tribological behavior of metal-polymer pairs in dry friction using the pin-on-disk scheme according to the method

[20]. Also, as a result of these model studies of the wear resistance of polymeric materials, their wear resistance characteristics  $C_2, m_2$  are given in Table 2.

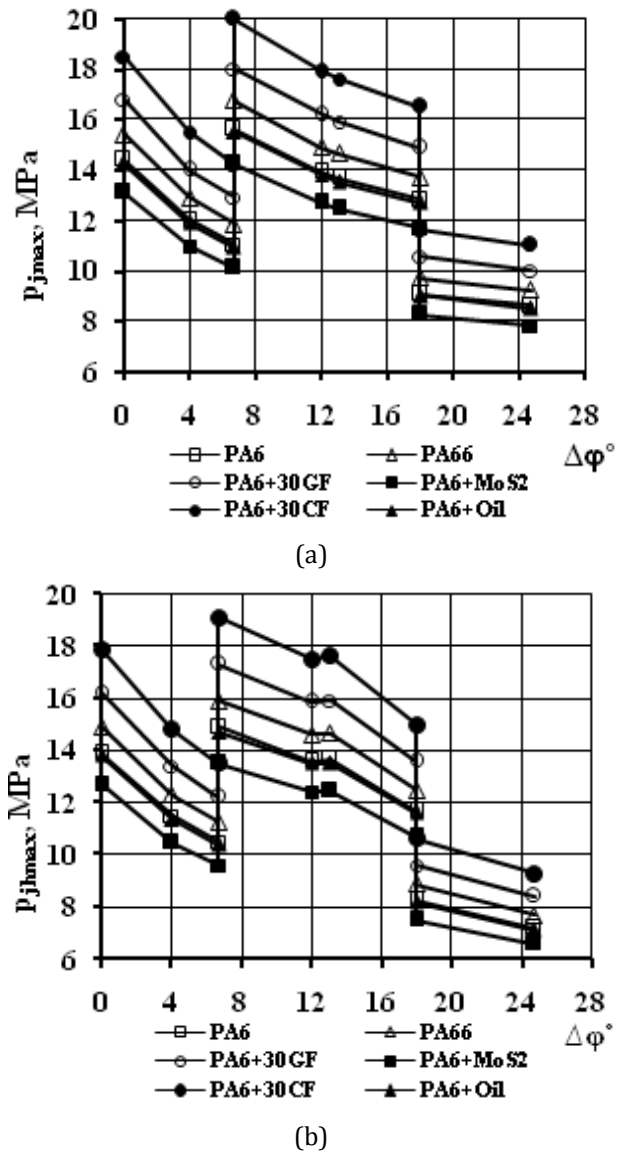
**Table 2.** Polyamides and composites based on them.

Wear resistance characteristics	Thermoplastic polymeric materials					
	PA6	PA66	PA6+30GF	PA6+MoS <sub>2</sub>	PA6+30CF	PA6+Oil
Linear wear resistance characteristic of gear material, $C_2 \cdot 10^6$	1.34	1.98	1.88	3.08	3.67	4.20
Power law wear resistance characteristic of gear material, $m_2$	1.15	1.15	1.15	1.15	1.15	1.15
Shear strength $\tau_s$ , MPa	40	40	50	38	40	38

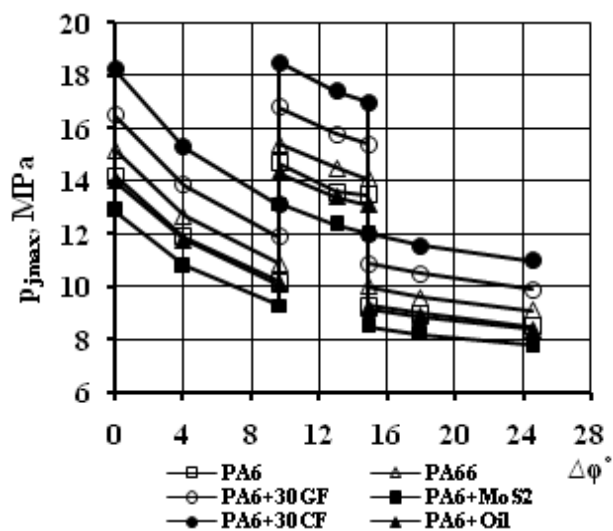
Note: the characteristics  $C$ ,  $m$  are established by the pin-on-disk scheme under dry friction at  $T = 23 \pm 1^\circ\text{C}$  and relative humidity of  $50 \pm 5\%$  (ISO 7148-2 standard [29]).

The results of studies for the influence of the helix angle on the maximum initial contact pressure and pressure after wear, the linear wear of tooth profiles, and gear durability are shown in Figs. 2 – 7. Figures 2-4 demonstrate the change in the initial maximum contact pressures  $p_{j\max}$  in the cycle of two-one-two-pair engagement ( $\beta = 0^\circ, 5^\circ$ ) (Figs. 2a and 3a) and three-two-three-pair engagement ( $\beta = 10^\circ$ ) (Fig. 4a). Accordingly, Fig. 2b, 3b, and 4b show contact pressures  $p_{jh\max}$  after wear when reaching the acceptable gear tooth wear  $h_{2^*} = 0.5$  mm at one of the points of engagement.

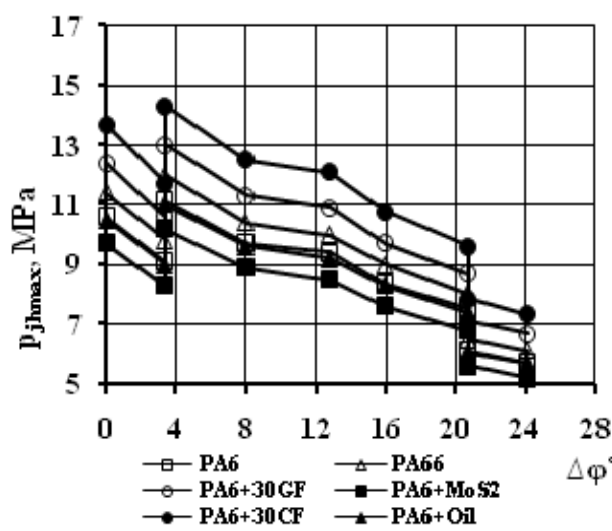
The figures on the left show the area of the left phase of two-pair ( $\beta = 0^\circ, 5^\circ$ ) or three-pair ( $\beta = 10^\circ$ ) engagement. The area changes with increasing the helix angle. In the case of two-one-two-pair engagement (Fig. 2a and 3a), with increasing the helix angle, the length of two-pair engagement increases and the length of one-pair engagement (central phase) decreases. Also, the length of the right phase of two-pair engagement increases. At  $\beta = 0^\circ$ , the pressure  $p_{j\max}$  at the teeth' entrance to the left phase of two-pair engagement will be slightly lower (by 1.09 times) than at the teeth' entrance to the one-pair engagement. At the helix angle  $\beta = 5^\circ$ , the highest  $p_{j\max}$  are close at these points of engagement of teeth and are 1.07 times lower than at  $\beta = 0^\circ$ . Accordingly, at  $\beta = 5^\circ$ , the total overlap ratio is  $\varepsilon_\gamma = \varepsilon_\alpha + \varepsilon_\beta = 1.741$  compared with the end overlap ratio  $\varepsilon_\alpha = 1.372$  at  $\beta = 0^\circ$ .



**Fig. 2.** Maximum contact pressures in the meshing at  $\beta = 0^\circ$ : a) before wear, b) after wear of the wheel teeth.

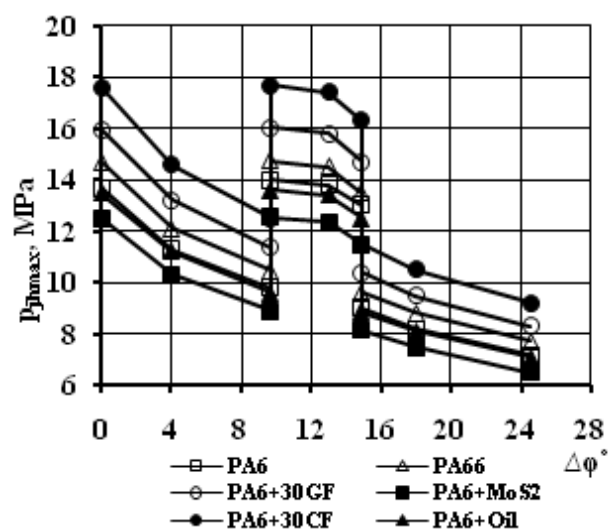


(a)



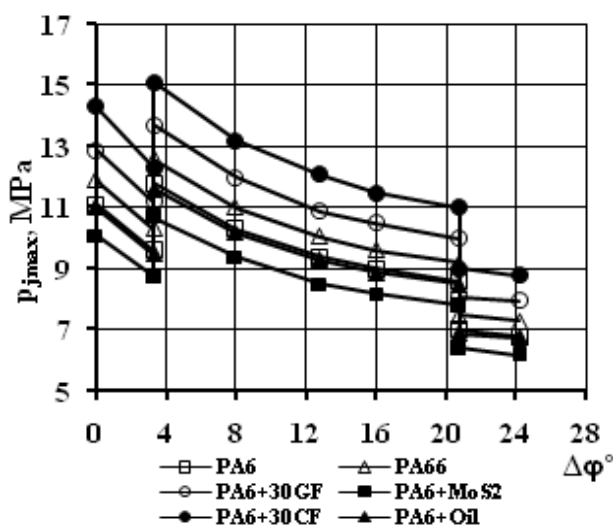
(b)

Fig. 4. Maximum contact pressures in the meshing at  $\beta = 10^\circ$ : a) before wear, b) after wear of the wheel teeth.



(b)

Fig. 3. Maximum contact pressures in the meshing at  $\beta = 5^\circ$ : a) before wear, b) after wear of the wheel teeth.



(a)

At a helix angle of  $\beta = 10^\circ$  there is observed a three-two-three-pair engagement with an overlap ratio of  $\varepsilon_\gamma = 2.033$ . Accordingly, the left and right areas of the three-pair engagement are narrow, while the central area of the two-pair engagement is large. The maximum contact pressures at the teeth' entrance to the left phase of the three-pair engagement is 1.07 times lower than that at the teeth' entrance to the two-pair engagement. On the other hand, the reduction in  $p_{jmax}$  in helical gears is up to by 1.33 times compared to the spur gears.

The research results demonstrate that the use of MoS<sub>2</sub> and oil fillers for the basic polyamide PA6 allows one to slightly lower the maximum contact pressures  $p_{jmax}$  in the engagement. When using 30% GF and 30% CF as fillers, the maximum contact pressures increase significantly. In particular, the ratio of maximum contact pressures in gears with a gear made of PA6+30CF relative to ones for unfilled polyamide PA6 is 1.28. In general, the pressure variation reaches 1.41 times (PA6+30CF relative to PA6+MoS<sub>2</sub>). Undoubtedly, this fact will also affect the durability of gears, which will be shown below.

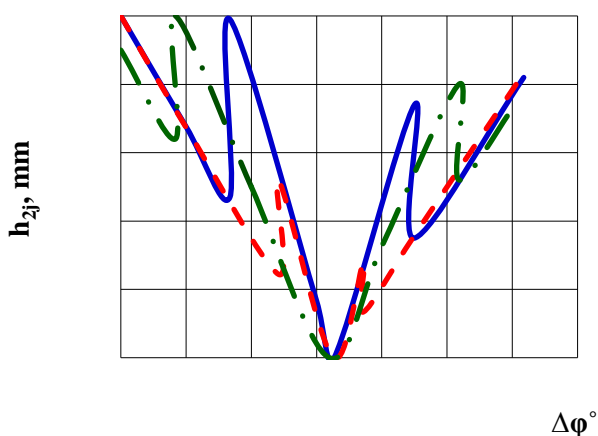
The important role of the composition of PA6-based composites in the change of contact pressures  $p_{jmax}$  confirms the decisive influence

of Young's modulus on  $p_{j\max}$ . The higher Young's modulus of the polymer material relative to PA6, the higher the contact pressures. Correspondingly, the pressures will be lower for smaller Young's moduli.

The wear of polymer gear teeth leads to a decrease in the pressure  $p_{j\max}$  at the entrance to the two-pair (three-pair) and one-pair (two-pair) engagement by  $\approx 1.055$  times, regardless of the helix angle, as shown in Figures 2b, 3b, and 4b. The tooth wear has a significantly greater impact on reduction in  $p_{j\max}$  at the exit from one-pair engagement and in the right phase of two-pair engagement (up to by 1.2 times).

On the other hand, the operation conditions of MP gears are significantly improved in helical gears compared to spur gears. It is because they have a much larger engagement area with a higher parity of the teeth contact, even at an angle of  $\beta = 5^\circ$  (Fig. 3a). At a helix angle of  $10^\circ$  (Fig. 4a) with three-two-three-pair engagement, the area of three-pair engagement is smaller than that of two-pair one.

The trend of the linear wear  $h_{2j}$  of polymer gear teeth at selected points of engagement depending on different helix angles is shown in Fig. 5.



**Fig. 5.** Linear wear of polymer gear tooth profile during engagement: solid line for  $\beta = 0^\circ$ , dashed line for  $\beta = 5^\circ$ , and dash-dotted line for  $\beta = 10^\circ$ .

In a spur gear, where  $\beta = 0$ , the acceptable wear  $h_{2^*} = 0.5$  mm of the gear teeth is reached at their entrance to the left phase of the two-pair engagement. At the entrance to the one-pair

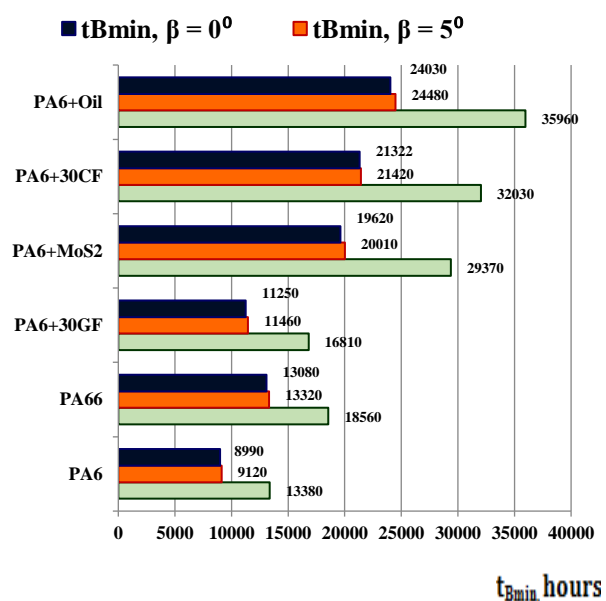
engagement, the tooth wear is close to the acceptable one. That is, at these two characteristic points of engagement, tooth wear is almost equal. At the exit of the teeth from the one-pair and the second phase of two-pair engagement, the wear is smaller.

In helical gears with the helix angle  $\beta = 5^\circ$ , the distribution of their wear will be somewhat different. The acceptable tooth wear will also be achieved at the entrance to the left phase of the two-pair engagement. At the entrance to the one-pair engagement (central zone) it will be significantly lower than that in spur gears. At the exit of teeth from the second phase of two-pair engagement, their wears will be close.

At the helix angle  $\beta = 10^\circ$  (three-two-three-pair engagement), the acceptable wear of teeth is achieved at the entrance to the two-pair engagement (central zone). At the exit of the teeth from the central and final phases of engagement, their wear will be close.

For all studied polyamides, patterns of the tooth linear wear presented in Fig. 5 are the same during the engagement phase.

On the contrary, the estimated minimum durability  $t_{B\min}$  of gears made of different types of polyamides will be significantly different depending on the helix angle (Fig. 6).



**Fig. 6.** Minimum durability of MP gears at different helix angles with the acceptable wear of gear teeth.



Minimum gear durability is the durability at the point of the tooth profile where the acceptable wear is reached (Fig. 5). It, as noted above, will occur at different points for different helix angles.

The lowest durability will be for gears made of unfilled polyamide PA6. The durability of gears made of PA6+30GF will be 1.25 times higher than that of PA6. The durability ratio of gears made of PA66 and PA6 is 1.46. The gears made of polyamide composites have significantly higher durability: PA6+MoS<sub>2</sub> by 2.19 times, PA6+30CF by 2.43 times), and PA6+Oil by 2.68 times.

Fig. 7 presents a relative evaluation of MP gears durability depending on the helix angle for gear made of different polymeric materials.

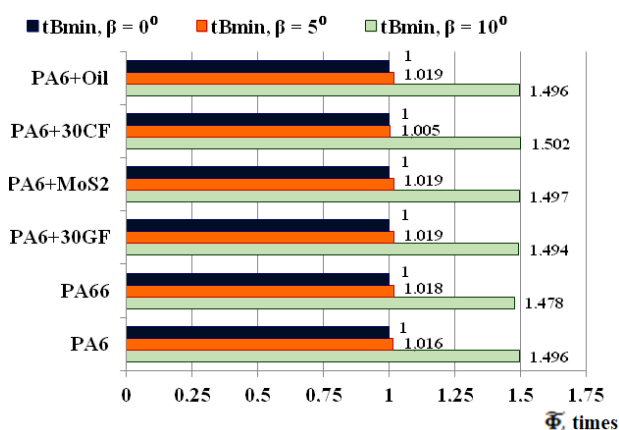


Fig. 7. The relative durability of MP gears at different helix angles.

In helical gears with a helix angle of  $\beta = 5^\circ$ , a slight increase in durability is achieved as compared to spur gears (up to by 1.019 times). This can be related to the slight decrease in the contact pressures  $p_{0\max}$  at the tooth entrance to the two-pair engagement at the angle  $\beta = 5^\circ$  compared to  $\beta = 0$  (point  $j = 0$ , where the acceptable  $h_{2^*} = 0.5$  mm is reached) (Fig. 5, Tables A1 and A2 in Appendices). For example, in gears made of PA6,  $p_{0\max} = 14.2$  MPa ( $\beta = 5^\circ$ ),  $p_{0\max} = 14.4$  MPa ( $\beta = 0$ ). Also, at a helix angle of  $\beta = 5^\circ$ , the total contact ratio  $\varepsilon_\gamma = \varepsilon_\alpha + \varepsilon_\beta = 1.741$ . It leads to a significant narrowing of the one-pair engagement phase (Fig. 2). At  $\beta = 0$ , the end overlap ratio  $\varepsilon_\alpha$

equals 1.372. At the helix angle  $\beta = 10^\circ$ , the durability of MP gears for all polymer materials studied increases by about 1.5 times due to the 1.225-fold decrease in contact pressure  $p_{2\max}$  in point  $j = 2$ , where  $h_{2^*} = 0.5$  mm is reached for three-two-three-pair engagement (Fig. 5, Table A3).

In the Appendix, the tables show the results of the calculations based on which the diagrams were built and analyzed.

#### 4. CONCLUSIONS

The basic qualitative regularities of the effect of tooth wear and engagement parity on maximum contact pressures, linear teeth wear along the profile, and resource of MP helical gears at different helix angles have been established.

1. The highest contact pressures occur in engagement when using PA6+30CF, and they are slightly lower for PA6+30GF. The level of pressure depends on Young's modulus, and it is the highest in these composites (Table 1). The lowest maximum pressures are characteristic for the composite PA6 + MoS<sub>2</sub>.
2. In spur gears, the linear wear of teeth is differentiated during their engagement. The point of engagement where the acceptable tooth wear is reached is located at the entrance to the left phase of the two-one-two-pair engagement. In helical gears, it is either at the entrance to the left phase of the two-one-two-pair engagement, or at the entrance to the central phase of the three-two-three-pair engagement.
3. At the helix angle  $\beta = 10^\circ$ , the gear durability increases significantly due to the occurrence of the three-two-three-pair engagement and the maximum contact pressure in the engagement decreases. The gears with PA6 polyamide gear have the lowest durability. The durability of MP gears with a gear made of polyamide composites PA6+MoS<sub>2</sub>, PA6+30CF, and PA6+Oil will be much higher. Filling of the base polyamide PA6 with different components makes it possible to increase the durability of MP gears by 2.68 times.

4. Important for engineering practice issues of assessing the teeth' contact strength at the most loaded contact points and predicting the gears' durability, as well as a very important task of optimal choice of polymer materials for MP gears according to these criteria have been effectively solved thanks to using the newly developed generalized (complex) analytical method. The method expands the possibilities of MP gears research in comparison with the calculation methods for metal gears given in the standards ISO 6336 - 2 [29], DIN 3900 [30], and VDI 2736 [31]. In particular, using the method at any point of teeth engagement makes it possible to assess the maximum contact pressure, sliding speed, radius of curvature of the tooth profile, linear wear of teeth, gear durability; to determine the angles of change in the engagement type (two-one-two-pair or three-two-three-pair), and the angle of the tooth exit from the engagement; to consider the influence of tooth wear on the change in the curvature radius of the profile, on contact pressures, and gear durability, and to consider the effect of gears correction (was not investigated in this article) on the contact and tribological characteristics of MP gears.

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## NOMENCLATURE

$a$	center distance of gear pair, mm	$2b_j$	width of contact area, mm
$B$	calculation block size, rev	$C_k, m_k$	wear resistance characteristics of gear materials, [-]
$b$	width of pinion, mm		

$E$	Young's modulus of gear tooth materials, MPa	$R_m$	immediate tensile strength of material, MPa
$f$	sliding friction coefficient, [-]	$r$	radius of gear tooth fillet, mm
$h_{k^*}$	acceptable wear of composite gear, mm	$r_1, r_2$	pitch circle radii of pinion and gear, respectively, mm
$h'_{kj}$	single linear wear of gear teeth at any $j$ -th point of tooth profile, mm	$r_{b1}, r_{b2}$	base circle radii of pinion and gear, respectively, mm
$h_{kjin}$	total wear of gear teeth, mm	$r_{a1}, r_{a2}$	addendum circle radii of pinion and gear, respectively, mm
$h_{kjB}$	wear of gear teeth in individual interaction block, mm	$l_{min}$	minimum contact line length, mm
$i = 1, 2, \dots$	load levels, [-]	$T_{nom}$	rated torque, Nmm
$j$	contact points on the active face of the teeth, [-]	$t'_j$	time of contact at displacement of the $j$ -th point of contact along tooth profile by contact area width $2b_j = const$ , sec
$j = 0, j = s$	the first and the last point of tooth engagement, respectively, [-]	$t_{B\ min}$	minimal durability as calculated by the block method, h
$K_g$	dynamic factor, [-]	$u$	gear ratio, [-]
$k = 1; 2$	number of gears (1 – pinion, 2 – gear)	$v_j = v$	sliding speed at the $j$ -th point of tooth profile, m/sec
$m$	engagement module, mm	$v_0$	velocity of the contact point along tooth profile, m/sec
$N$	force acting in tooth engagement, N	$w$	number of engaged tooth pairs, [-]
$n_1$	number of pinion revolutions, rpm	$Z_1, Z_2$	numbers of pinion teeth and gear teeth, respectively, [-]
$P$	power on drive shaft (pinion), kW		
$p_b$	pitch of teeth, mm		
$p_{j\ max}$	maximum contact pressure at the $j$ -th point of contact, MPa		
$p_{jh\ max}$	maximum tribocontact pressure (for tooth wear) at the $j$ -th point of contact, MPa		

### Greek letters

$\alpha$	pressure angle of engaged teeth, °	$\rho_j$	reduced curvature radius of gear profile due to wear, in a normal section, mm
$\alpha_t$	end pressure angle, °	$\rho_{1j}, \rho_{2j}$	initial curvature radii of the profiles of pinion teeth and gear teeth, respectively, mm
$\alpha_{t10}$	angle of the first point on contact line,	$\rho_{jh}$	reduced curvature radius of the gear profile due to wear, mm
$\alpha_{t1s}$	angle describing location of the last point of engagement of pinion teeth on contact line, °	$\rho_{1jh}, \rho_{2jh}$	variable curvature radii of the profiles of pinion teeth and gear teeth, respectively, mm
$\alpha_{t20}, \alpha_{t2s}$	angles describing location of the first and last points of engagement of gear teeth on contact line, °	$\tau_s$	shear strength of material, MPa
$\beta$	helix angle, °	$T_{j\ max}$	maximum specific friction force according to Coulomb's law, MPa
$\Delta\varphi$	selected angle of rotation of pinion teeth from the point of initial contact (point 0) to point 1, and so on, °	$\varepsilon_\alpha, \varepsilon_\beta$	gear end and pitch overlap ratios, respectively, [-]
$\mu$	Poisson's ratio of gear tooth materials, [-]	$n_\alpha, n_\beta$	fractional parts of end and pitch overlap ratios, respectively, [-]
$\omega_1$	angular velocity of pinion, sec <sup>-1</sup>		

Appendices

Table A1

$\beta = 0$	Parameters									
Polymers		$j=0$	$j=1$	$j=2$	$j=2$	$j=3$	$j=4$	$j=5$	$j=5$	$j=6$
PA6	$p_{jmax}$ , MPa	14.4	12	11.05	15.6	13.9	13.65	12.8	9.05	8.6
	$p_{jhmax}$ , MPa	13.9	11.5	10.5	14.9	13.6	13.65	11.7	8.26	7.2
	$h_{2j}$ , mm	0.5	0.338	0.235	0.495	0.083	0	0.37	0.175	0.41
	$t_{Bmin}$ , hours	8990								
	$\Delta\varphi$ , °	0	4	6.69	6.69	12	13.08	18	18	24.7
PA66	$p_{jmax}$ , MPa	15.4	12.9	11.84	16.74	14.9	14.64	13.7	9.7	9.2
	$p_{jhmax}$ , MPa	14.9	12.3	11.28	15.9	14.6	14.64	12.5	8.86	7.7
	$h_{2j}$ , mm	0.5	0.338	0.235	0.495	0.083	0	0.37	0.175	0.41
	$t_{Bmin}$ , hours	13080								
	PA6+30GF	$p_{jmax}$ , MPa	16.8	14	12.9	18.2	16.2	15.9	14.9	10.55
$p_{jhmax}$ , MPa		16.2	13.4	12.2	17.31	15.85	15.9	13.6	9.6	8.4
$h_{2j}$ , mm		0.5	0.338	0.235	0.495	0.083	0	0.37	0.175	0.41
$t_{Bmin}$ , hours		11250								
PA6+MoS <sub>2</sub>		$p_{jmax}$ , MPa	13.1	10.96	10.1	14.25	12.7	12.45	11.7	8.25
	$p_{jhmax}$ , MPa	12.7	10.46	9.6	13.5	12.4	12.45	10.7	7.5	6.6
	$h_{2j}$ , mm	0.5	0.338	0.235	0.495	0.083	0	0.37	0.175	0.41
	$t_{Bmin}$ , hours	19620								
	PA6+30CF	$p_{jmax}$ , MPa	18.5	15.5	14.2	20.1	17.9	17.6	16.5	11.6
$p_{jhmax}$ , MPa		17.9	14.8	13.5	19.1	17.5	17.6	15	10.6	9.3
$h_{2j}$ , mm		0.5	0.338	0.235	0.495	0.083	0	0.37	0.175	0.41
$t_{Bmin}$ , hours		21532								
PA6+Oil		$p_{jmax}$ , MPa	14.25	11.9	10.9	15.5	13.8	13.5	12.7	9
	$p_{jhmax}$ , MPa	13.8	11.35	10.4	14.7	13.5	13.5	11.6	8.2	7.1
	$h_{2j}$ , mm	0.5	0.338	0.235	0.495	0.083	0	0.37	0.175	0.41
	$t_{Bmin}$ , hours	24030								

Table A2

$\beta = 5^\circ$	Parameters									
Polymers		$j=0$	$j=1$	$j=2$	$j=2$	$j=3$	$j=4$	$j=5$	$j=5$	$j=6$
PA6	$p_{jmax}$ , MPa	14.2	11.9	10.2	14.7	13.6	13.5	9.3	9	8.5
	$p_{jhmax}$ , MPa	13.7	11.3	9.8	14.4	13.6	13.2	9.0	8.2	7.15
	$h_{2j}$ , mm	0.5	0.337	0.122	0.26	0	0.14	0.067	0.179	0.412
	$t_{Bmin}$ , hours	9120								
	$\Delta\varphi$ , °	0	4	9.67	9.67	13.01	14.87	14.87	18	24.57
PA66	$p_{jmax}$ , MPa	15.2	12.7	10.9	15.4	14.5	14.1	10	9.6	9.1
	$p_{jhmax}$ , MPa	14.7	12.1	10.45	14.75	14.5	13.5	9.6	8.8	7.7
	$h_{2j}$ , mm	0.5	0.337	0.122	0.26	0	0.14	0.067	0.179	0.412
	$t_{Bmin}$ , hours	13320								
	PA6+30GF	$p_{jmax}$ , MPa	16.5	13.85	11.9	16.8	15.8	15.4	10.9	10.5
$p_{jhmax}$ , MPa		15.95	13.2	11.35	16.05	15.8	14.7	10.4	9.5	8.3

	$h_{2j}$ , mm	0.5	0.337	0.122	0.26	0	0.14	0.067	0.179	0.412
	$t_{Bmin}$ , hours	11460								
PA6+MoS <sub>2</sub>	$p_{jmax}$ , MPa	12.9	10.8	9.3	13.15	12.35	12	8.5	8.2	7.8
	$p_{jhmax}$ , MPa	12.5	10.3	8.9	12.55	12.35	11.5	8.15	7.5	6.5
	$h_{2j}$ , mm	0.5	0.337	0.122	0.26	0	0.14	0.067	0.179	0.412
	$t_{Bmin}$ , hours	20010								
PA6+30CF	$p_{jmax}$ , MPa	18.25	15.3	13.1	18.5	17.4	17	12	11.55	11
	$p_{jhmax}$ , MPa	17.6	14.6	12.5	17.7	17.4	16.3	11.5	10.5	9.2
	$h_{2j}$ , mm	0.5	0.337	0.122	0.26	0	0.14	0.067	0.179	0.412
	$t_{Bmin}$ , hours	21420								
PA6+Oil	$p_{jmax}$ , MPa	14	11.8	10.1	14.3	13.4	13.1	9.2	8.9	8.4
	$p_{jhmax}$ , MPa	13.5	11.2	9.6	13.6	13.4	12.5	8.85	8.1	7.1
	$h_{2j}$ , mm	0.5	0.337	0.122	0.26	0	0.14	0.067	0.179	0.412
	$t_{Bmin}$ , hours	24480								

Table A3

$\beta = 10^\circ$ Polymers	Parameters									
		$j=0$	$j=1$	$j=2$	$j=2$	$j=3$	$j=4$	$j=5$	$j=5$	$j=6$
PA6	$p_{jmax}$ , MPa	11.1	9.6	11.8	10.3	9.4	9	8.6	7	6.8
	$p_{jhmax}$ , MPa	10.6	9.1	11.15	9.7	9.4	8.35	7.5	6.1	5.7
	$h_{2j}$ , mm	0.45	0.32	0.5	0.25	0	0.163	0.4	0.26	0.37
	$t_{Bmin}$ , hours			13380						
	$\Delta\varphi$ , °	0	3.35	3.35	8	12.78	16	20.73	20.73	24.165
PA66	$p_{jmax}$ , MPa	11.9	10.3	12.6	11	10.05	9.6	9.2	7.5	7.3
	$p_{jhmax}$ , MPa	11.4	9.8	12	10.4	10	9	8	6.5	6.1
	$h_{2j}$ , mm	0.45	0.32	0.5	0.25	0	0.163	0.4	0.26	0.37
	$t_{Bmin}$ , hours			18470						
PA6+30GF	$p_{jmax}$ , MPa	12.9	11.2	13.7	12	10.9	10.5	10	8.1	7.95
	$p_{jhmax}$ , MPa	12.4	10.6	13	11.3	10.9	9.7	8.7	7.1	6.7
	$h_{2j}$ , mm	0.45	0.32	0.5	0.25	0	0.163	0.4	0.26	0.37
	$t_{Bmin}$ , hours			16810						
PA6+MoS <sub>2</sub>	$p_{jmax}$ , MPa	10.1	8.75	10.7	9.4	8.5	8.2	7.8	6.4	6.2
	$p_{jhmax}$ , MPa	9.7	8.3	10.2	8.9	8.5	7.6	6.8	5.6	5.2
	$h_{2j}$ , mm	0.45	0.32	0.5	0.25	0	0.163	0.4	0.26	0.37
	$t_{Bmin}$ , hours			29370						
PA6+30CF	$p_{jmax}$ , MPa	14.3	12.3	15.1	13.2	12.1	11.5	11	9	8.8
	$p_{jhmax}$ , MPa	13.7	11.7	14.3	12.5	12.1	10.75	9.6	7.85	7.35
	$h_{2j}$ , mm	0.45	0.32	0.5	0.25	0	0.163	0.4	0.26	0.37
	$t_{Bmin}$ , hours			32030						
PA6+Oil	$p_{jmax}$ , MPa	11	9.5	11.6	10.2	9.3	8.9	8.5	6.9	6.75
	$p_{jhmax}$ , MPa	10.5	9	11	9.6	9.2	8.3	7.4	6.05	5.7
	$h_{2j}$ , mm	0.45	0.32	0.5	0.25	0	0.163	0.4	0.26	0.37
	$t_{Bmin}$ , hours			35960						